MIND MAP: LEARNING MADE SIMPLE CHAPTER - 10

If λ Multiplied to vector AB, then the magnitude is multiplied by $|\lambda|$ and direction remain same (or opp.) according as λ is the + ve or , -ve.

A quantity that has both magnitude and direction is called a vector. The distance between the initial and terminal points of a vector is called its magnitude. Magnitude of vector \overrightarrow{AB} is |AB|.

For a given vector \hat{a} , the vector $\hat{a} = \frac{a}{|a|}$ gives the unit vector in the direction of *a*. for eg, if a=5i, then $\hat{a} = \frac{5i}{|5|} = i$, which is a unit vector. Position vector of a point P(x, y, z) is $x\hat{i} + y\hat{j} + z\hat{k}$ and its magnitude is $OP(r) = \sqrt{x^2 + y^2 + z^2}$. For eg: Position vector of P(2,3,5) is $2\hat{i} + 3\hat{j} + 5\hat{k}$ and its magnitude is $\sqrt{2^2 + 3^2 + 5^2} = \sqrt{38}$.

The Position vector of a point R dividing a line segment joining *P*, *Q* whose position vectors are *a*, *b* resp., in the ratio m: n (i) internally is $\frac{na+mb}{m}$, (ii) externally is $\frac{mb-na}{m}$

Manual of vector by a scalar Direction ratios and Ju direction cosines

Vector

Algebra

Properties of Vector

The scalar components of a vector are its direction ratios, and represent its projections along the respective axes.

If a, b are the vectors and ' θ ', angle between Cross Product of two vectors them, then their scalar product $a.b = |a||b|\cos\theta$ $\Rightarrow \cos \theta = -\frac{1}{2}$

The magnitude (r) direction ratios (a,b,c) and direction cosines (l,m,n) of vector $a\hat{i} + b\hat{j} + c\hat{k}$ are related as:

 $l = \frac{a}{m}, m = \frac{b}{m}, n = \frac{c}{m}$

For eg: If $\overrightarrow{AB} = \hat{i} + 2\hat{j} + 3\hat{k}$, then $r = \sqrt{1 + 4 + 9} = \sqrt{14}$

Direction ratios are (1,2,3) $\left(\sqrt{\frac{1}{14}},\sqrt{\frac{2}{14}},\sqrt{\frac{3}{14}}\right)$ and direction cosines are

 $a \times b = |a||b|\sin\theta \hat{n}, \hat{n}$ is a unit vector perpendicular to line joining *a,b*.

- (i) Zero vector (initial and terminal points coincide)
- (ii) Unit vector (magnitude is unity)
- (iii) Coinitial vectors (same initial points)
- (iv) Collinear vectors (parellel to the same line)
- (v) Equal vectors (same magnitude and direction)
- (vi) Negative of a vector (same magnitude, opp. direction)

If we have two vectors $a = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}, b = b_1\hat{i} + b_2\hat{j} + b_3\hat{k}$ and λ is any scalar, then $a+b=(a_1+b_1)\hat{i}+(a_2+b_2)\hat{j}+(a_3+b_3)\hat{k}$

$$a+b = (a_1 + b_1)\hat{i} + (a_2 + b_2)\hat{j} + (a_3 + b_3)\hat{k}$$

$$\lambda a = (\lambda a_1)\hat{i} + (\lambda a_2)\hat{j} + (\lambda a_3)\hat{k}$$

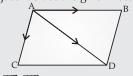
$$a.b = a_1b_1 + a_2b_2 + a_3b_3 \text{ and}$$

$$a \times b = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \end{vmatrix}$$

The Vector sum of two coinitials vectors is given by the diagonal of the parallelogram whose adjacent sides are given vectors.

scalar product of

two vectors



if \overrightarrow{AB} , \overrightarrow{AC} are the given vectors, then $\overrightarrow{AB} + \overrightarrow{AC} = \overrightarrow{AD}$

The vector sum of the three sides of a triangle taken in order is 0.i.e

if ABC is given triangle, then $\overrightarrow{AB} + \overrightarrow{BC} + \overrightarrow{CA} = 0$.

